Assessment Schedule - 2008

Physics: Demonstrate understanding of mechanical systems (90521)

Evidence Statement

Q	Evidence	Achievement	Achievement with Merit	Achievement with Excellence
ONE (a)	$\tau = Fr = 132 \text{ N} \times 0.83 \text{ m} = 109.56 \text{ [= 110 Nm (2sf)]}$	² SHOW question. Correct working shown.		
(b)	$\tau = I\alpha$ $I = \frac{\tau}{\alpha} = \frac{110}{0.48} = 229 = 230 \text{ kg m}^2$ If you use 109.56 you get 228.25.	² SHOW question. Correct working.		
(c)	final $E_{K(ROT)} = \frac{1}{2}I\omega^2$ = $\frac{1}{2} \times 230 \times 0.58^2$ = 39 J (2 sf) OR 38 J (2sf) (109.56 × 0.35) = 38.39 J)	2 Correct numerical answer for $E_{\rm k}$.	If uses work = 109.56×0.35 OR uses $I = 228.25$ then rounding will be 38 J Otherwise 39 J	
	Correct sf and units	1		
(d)	The force moved a distance : so work (Fd) was done that transferred energy to the door. (assuming F constant) OR the force caused a torque ($\tau = Fr$) which moved through an angle so work ($\tau\theta$) was done and transferred energy . (1) Links force to work in context. $F \to \tau \to work^{(a)} \to \Delta KE$ $F \to work^{(b)} \to \Delta KE$ (a) work could be torque and rotation / angle / tuning (b) work is force and distance moved. (2) Links work to change in energy. Work causes the (change in) energy (kinetic energy). (3) Links force to acceleration and then work. $F \to \tau \to \alpha \to \Delta\omega \to (\Delta)KE$ Argument must be a rotational one (not linear).		Any of (1) OR (2) OR (3) If have not explained the gain in KE of the door OR explanation (3) is almost complete.	BOTH of (1) AND (2) OR (3) They must explain the gain in KE for Excellence

(e)	Yes because: If torque is the same, as $\tau = Fr$, if r is bigger, F is smaller The reason why torque must be the same is because this causes - same time and same velocity - or the same angular acceleration.		Torque constant and therefore as radius (r) increases F decreases	1 Justifies why the torque must be constant, eg: - Constant τ gives angular acceleration. OR - Constant τ gives same time and same velocity
(f)	Angle travelled during acceleration $\omega_f^2 = \omega_i^2 + 2\alpha\theta \omega_i = 0$ $\frac{\omega_f^2}{2\alpha} = \theta = \frac{0.58^2}{2 \times 0.48} = 0.35 \text{ radian}$ so after she stops pushing angle is $2.0 - 0.35 = 1.65 \text{ rad.}$	² Correct calc of angle travelled during acceleration. (0.35 rad)	² Correct answer.	
(g)	$t_{tot} = t_1 + t_2$ $t_1 \text{ is the time to accelerate}$ $\omega_f = \omega_i + \alpha t \text{ or similar}$ $t_1 = \frac{\omega}{\alpha}$ $t_2 \text{ is the time to rotate freely}$ $use \ \omega = \frac{\Delta \theta}{\Delta t} \text{ or similar}$ $t_2 = \frac{\theta_2}{\omega}$ So $t_{total} = \frac{\omega}{\alpha} + \frac{\theta_2}{\omega}$	SHOW question ¹ States or implies that $t_{total} = t_{acc} + t_{const}$ Substitution with values (N).	Derives one of the two terms correctly. Derives means to take from one form to another form OR shows a step from something else to this.	¹ Correct answer.
TWO (a)	Reaction from suspension cable Weight of chairs	¹ Forces correctly labelled Can be through COM. (should be roughly equal in length).		

(b)	Chair moves because of unbalanced torque. Due to centre of mass to the right of the suspension cable / weight of skier causes torque.	¹ Any of:	¹ Reason for movement	¹ Reason for equilibrium
	Torque is force × distance between the line of action of the force and the pivot. Net torque causes angular acceleration. Hangs in new position where new centre of mass is below suspension point, so there is no net torque and no angular acceleration.	COM moved to the right (towards X) The new COM now (moved to be) below the suspension point	Produces a torque	Gives reason why the chair is in equilibrium using torques (see below)
		Weight of person causes a torque A "couple: causes a torque	Torque causes rotation of the chair (in clockwise direction) about pivot	Justifies why the COM is now under the pivot - balanced torque - no resultant torque

THREE			V _{max} SHM		
(c)			1.5 or uses cos formula	2.69	
		1.0	48° .78 rads $t = 0.361 \text{ s}$	68° 1.19 rads t = 0.551 s	
	$V_{ m max}$ Linear	1.2	37° 0.64 rads $t = 0.296 \text{ s}$	64° 1.11 rads t = 0.514 s	
		0.2	82° 1.43 rads $t = 0.662$ s	86° 1.50 rads t = 0.695 s	
		1.4	E2 21° 0.37 rads t = 0.162 s	59° 1.0 2rads t = 0.472 s	

THREE (a)	$T = 2 \sqrt{\frac{l}{g}}$ $T = 2 \sqrt{\frac{2.1}{9.81}} = 2\pi \times 0.46291 = 2.9070 = 2.9 \text{ s}$	A SHOW question ² Correct substitution into correct equation		
(b)	$\omega = 2$ $f = \frac{2}{t} = \frac{2}{0.91} = 2.16 \text{ rad s}^{-1}$ $V_{\text{max}} = r\omega$ $= 0.69 \times 2.16 = 1.49 \text{ m s}^{-1}$ Max speed is when the swing and the whole chair are going up: $V = 1.5 + 1.2 = 2.7 \text{ m s}^{-1}$	2 ω correctly calculated OR Adds their (incorrect) $V_{\rm max}$ to $1.2{\rm ms}^{-1}$	2 V_{max} =1.49 ms $^{-1}$ OR Consistent V_{max} calculated from their incorrect ω	² Correct answer 2.7 ms ⁻¹

(c)	The chair will be travelling at 0.2 m s^{-1} down hill velocity when its velocity relative to the equilibrium position is $1.2 + 0.2 \text{ m s}^{-1}$ down the hill. ie when $v \text{ is } 1.4 \text{ m s}^{-1}$ to the right relative to the pivot. $v = A\omega \cos \omega t$ $1.4 = 0.69 \times 2.16 \times \cos \omega t$ $\omega t = \cos^{-1} \left(\frac{1.4}{0.69 \times 2.16} \right) = 0.35 \text{ rad} = 20^{\circ} \text{ OR } 21^{\circ}$ Angle from eqm position is 20° either side of the max downhill velocity.	² Correct calculation of v relative to the pivot. (1.4 m s ⁻¹)	² Consistent answer from an incorrect Vmax OR uses sin (instead of cos) to get 70° (1.22 or 1.21 rads)	² Correct answer of 20° or 21°.
(d)	The state of the s	¹ Graph shows amplitude decreasing over 4 oscillations.	¹ Achieved and starts the graph at correct position AND shows period is the same.	

FOUR (a)	$F = \frac{GMm}{r^2} = \frac{6.67 \times 10^{-11} \times 5.97 \times 10^{24} \times 3.0 \times 10^{-3}}{\left[(6.38 + 0.35) \times 10^6 \right]^2}$ $= 2.6 \times 10^{-2} \text{ N}$ $(= 2.63749 \times 10^{-2} \text{ N})$	² Correct radius used (6.73 x 10 ⁶ m)	² Correct answer.	Watch for 0.029348N (N)
(c)(i)	For a stable orbit (1) centripetal force = gravitational force (Stability) (2) $\frac{mv^2}{r} = \frac{GMm}{r^2}$ (mass) m 's cancel so orbit speed is independent of mass (3) acceleration due to gravity is independent of mass, so the two objects so both (free) fall at same rate towards Earth - so they stay together (mass) (4) $v^2 = \frac{GM}{r}$ or $v^2 \alpha \frac{1}{r}$ so same radius gives same velocity (Same Velocity) Momentum gained by the ball $p = mv = 3 \times 10^{-3} \times 60 = 0.18 \text{ kg m s}^{-1}$, this equals momentum lost.	1 Uses: (1) Stability argument OR Explains why speed is constant, eg there is no friction. Force of gravity is at right angles to velocity. 2 Correct calculation of <i>p</i> (0.18 kgm/s) OR Correct direction Accept either directions: Δ <i>p</i> or mtm loss	1 Uses: (2) or (3) Mass argument made OR (4) Same velocity argument. 2 Both magnitude and direction correct Accept either directions: Δp or mtm loss	1 Uses: (4) Same velocity argument AND Mass argument (2) or (3)
(c)(ii)	Initial $p = 40 \times 0.2 = 8 \text{ kg m s}^{-1}$ to the right. 8 kg m s^{-1} 0.18cms^{-1} $0.18 \text{sin}^{-3} 0.18 \text{ kg m s}^{-1}$ $p_{\text{final}}^2 = (8 - 0.18 \text{cos}^{-3} 0)^2 + (18 \text{sin}^{-3} 0)^2 = 61.5$ $v = \frac{p_{\text{final}}}{m} = \frac{7.85}{0.2} = 39.25 \text{ m s}^{-1} \text{ (or use cosine rule)}$ $\theta = \tan^{-1} \left(\frac{0.18 \text{sin}^{-3} 0}{8 - 0.18 \text{cos}^{-3} 0} \right) = 0.88^{\circ}$	² Has incorrect vector diagram but uses it to give some explanation about why change is negligible Must use mtm diagram as part of their explanation (not just a velocity diagram)	² A correct consistent vector diagram or analysis (from 4c(i)	² A correct vector diagram or analysis and uses correct explanation about why change negligible

(c)(iii)	Because (in the collision) the change of momentum of the club head and the golf ball is unchanged and the ball is much lighter, the gain in speed of the ball is much greater than the decrease in v of the club head. or The club and the head experience the same force. However as the mass of the club head is greater than the mass of the ball the acceleration of the ball will be higher $(F = ma)$	¹ States that momentum is conserved	of mtm of golf club head to golf balls velocity Or Mentions that any of these is the same in collision -F force -Ft impulse -Δp change in mtm. on ball and club head	
(d)	As he starts to rotate the club, he will rotate in the opposite direction (the total angular momentum will remain constant). As he hits the ball, he will recoil (total linear momentum will remain constant).	¹ Rotation or Translation Watch for incorrect directions (N)		

Judgement Statement

Achievement	Achievement with Merit	Achievement with Excellence
4×A1	$4 \times A1 + 2 \times M1$	$4 \times A1 + 2 \times M1 + 1 \times E1$
5 × A2	$4 \times A2 + 3 \times M2$	$4 \times A2 + 2 \times M2 + 1 \times E2$